

Chapter 6 - Arrays

Outline

- 6.1 **Introduction**
- 6.2 **Arrays**
- 6.3 **Declaring Arrays**
- 6.4 **Examples Using Arrays**
- 6.5 **Passing Arrays to Functions**
- 6.6 **Sorting Arrays**
- 6.7 **Case Study: Computing Mean, Median and Mode Using Arrays**
- 6.8 **Searching Arrays**
- 6.9 **Multiple-Subscripted Arrays**

Objectives

- In this chapter, you will learn:
 - To introduce the array data structure.
 - To understand the use of arrays to store, sort and search lists and tables of values.
 - To understand how to define an array, initialize an array and refer to individual elements of an array.
 - To be able to pass arrays to functions.
 - To understand basic sorting techniques.
 - To be able to define and manipulate multiple subscript arrays.



6.1 Introduction

- Arrays
 - Structures of related data items
 - Static entity – same size throughout program
 - Dynamic data structures discussed in Chapter 12

6.2 Arrays

- Array
 - Group of consecutive memory locations
 - Same name and type
- To refer to an element, specify
 - Array name
 - Position number
- Format:

$$\text{arrayname}[\text{position number}]$$
 - First element at position 0
 - n element array named c:
 - $c[0], c[1] \dots c[n - 1]$

Name of array (Note that all elements of this array have the same name, c)

| | |
|--------------|------|
| \downarrow | |
| $c[0]$ | -45 |
| $c[1]$ | 6 |
| $c[2]$ | 0 |
| $c[3]$ | 72 |
| $c[4]$ | 1543 |
| $c[5]$ | -89 |
| $c[6]$ | 0 |
| $c[7]$ | 62 |
| $c[8]$ | -3 |
| $c[9]$ | 1 |
| $c[10]$ | 6453 |
| $c[11]$ | 78 |

\uparrow
Position number of
the element within
array c

6.2 Arrays

- Array elements are like normal variables

```
c[ 0 ] = 3;  
printf( "%d", c[ 0 ] );
```

- Perform operations in subscript. If x equals 3

```
c[ 5 - 2 ] == c[ 3 ] == c[ x ]
```

6.2 Arrays

| Operators | | | | | | Associativity | Type |
|--------------------------------------|-----|----|-----------------|----|----|---------------|----------------|
| [] | () | | | | | left to right | highest |
| ++ | -- | ! | (<i>type</i>) | | | right to left | unary |
| * | / | % | | | | left to right | multiplicative |
| + | - | | | | | left to right | additive |
| < | <= | > | >= | | | left to right | relational |
| == | != | | | | | left to right | equality |
| && | | | | | | left to right | logical and |
| | | | | | | left to right | logical or |
| ?: | | | | | | right to left | conditional |
| = | += | -= | *= | /= | %= | right to left | assignment |
| , | | | | | | left to right | comma |
| Fig. 6.2 Operator precedence. | | | | | | | |

6.3 Defining Arrays

- When defining arrays, specify

- Name
 - Type of array
 - Number of elements

```
arrayType arrayName[ numberOfElements ];
```

- Examples:

```
int c[ 10 ];
```

```
float myArray[ 3284 ];
```

- Defining multiple arrays of same type

- Format similar to regular variables

- Example:

```
int b[ 100 ], x[ 27 ];
```

6.4 Examples Using Arrays

- Initializers

```
int n[ 5 ] = { 1, 2, 3, 4, 5 };
```

- If not enough initializers, rightmost elements become 0

```
int n[ 5 ] = { 0 }
```

- All elements 0

- If too many a syntax error is produced syntax error

- C arrays have no bounds checking

- If size omitted, initializers determine it

```
int n[ ] = { 1, 2, 3, 4, 5 };
```

- 5 initializers, therefore 5 element array



Outline

fig06_03.c

```
1 /* Fig. 6.3: fig06_03.c
2   initializing an array */
3 #include <stdio.h>
4
5 /* function main begins program execution */
6 int main()
7 {
8     int n[ 10 ]; /* n is an array of 10 integers */
9     int i;         /* counter */
10
11    /* initialize elements of array n to 0 */
12    for ( i = 0; i < 10; i++ ) {
13        n[ i ] = 0; /* set element at location i to 0 */
14    } /* end for */
15
16    printf( "%s%13s\n", "Element", "value" );
17
18    /* output contents of array n in tabular format */
19    for ( i = 0; i < 10; i++ ) {
20        printf( "%7d%13d\n", i, n[ i ] );
21    } /* end for */
22
23    return 0; /* indicates successful termination */
24
25 } /* end main */
```



Outline

Program Output

| Element | value |
|---------|-------|
| 0 | 0 |
| 1 | 0 |
| 2 | 0 |
| 3 | 0 |
| 4 | 0 |
| 5 | 0 |
| 6 | 0 |
| 7 | 0 |
| 8 | 0 |
| 9 | 0 |

6.4 Examples Using Arrays

- Character arrays
 - String “first” is really a static array of characters
 - Character arrays can be initialized using string literals

```
char string1[] = "first";
```

 - Null character '\0' terminates strings
 - string1 actually has 6 elements
 - It is equivalent to
 - Can access individual characters

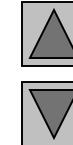
```
string1[ 3 ] is character 's'
```
 - Array name is address of array, so & not needed for scanf

```
scanf( "%s", string2 );
```

 - Reads characters until whitespace encountered
 - Can write beyond end of array, be careful



```
1 /* Fig. 6.4: fig06_04.c
2   Initializing an array with an initializer list */
3 #include <stdio.h>
4
5 /* function main begins program execution */
6 int main()
7 {
8     /* use initializer list to initialize array n */
9     int n[ 10 ] = { 32, 27, 64, 18, 95, 14, 90, 70, 60, 37 };
10    int i; /* counter */
11
12    printf( "%s%13s\n", "Element", "value" );
13
14    /* output contents of array in tabular format */
15    for ( i = 0; i < 10; i++ ) {
16        printf( "%7d%13d\n", i, n[ i ] );
17    } /* end for */
18
19    return 0; /* indicates successful termination */
20
21 } /* end main */
```



Outline

fig06_04.c



Outline

Program Output

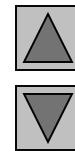
| Element | value |
|---------|-------|
| 0 | 32 |
| 1 | 27 |
| 2 | 64 |
| 3 | 18 |
| 4 | 95 |
| 5 | 14 |
| 6 | 90 |
| 7 | 70 |
| 8 | 60 |
| 9 | 37 |



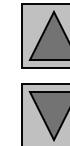
Outline

fig06_05.c

```
1 /* Fig. 6.5: fig06_05.c
2   Initialize the elements of array s to the even integers from 2 to 20 */
3 #include <stdio.h>
4 #define SIZE 10
5
6 /* function main begins program execution */
7 int main()
8 {
9   /* symbolic constant SIZE can be used to specify array size */
10  int s[ SIZE ]; /* array s has 10 elements */
11  int j;          /* counter */
12
13  for ( j = 0; j < SIZE; j++ ) { /* set the values */
14    s[ j ] = 2 + 2 * j;
15  } /* end for */
16
17  printf( "%s%13s\n", "Element", "Value" );
18
19  /* output contents of array s in tabular format */
20  for ( j = 0; j < SIZE; j++ ) {
21    printf( "%7d%13d\n", j, s[ j ] );
22  } /* end for */
23
24  return 0; /* indicates successful termination */
25
26 } /* end main */
```

Outline**Program Output**

| Element | value |
|---------|-------|
| 0 | 2 |
| 1 | 4 |
| 2 | 6 |
| 3 | 8 |
| 4 | 10 |
| 5 | 12 |
| 6 | 14 |
| 7 | 16 |
| 8 | 18 |
| 9 | 20 |



Outline

fig06_06.c

```

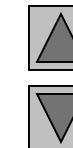
1  /* Fig. 6.6: fig06_06.c
2      Compute the sum of the elements of the array */
3  #include <stdio.h>
4  #define SIZE 12
5
6  /* function main begins program execution */
7  int main()
8 {
9     /* use initializer list to initialize array */
10    int a[ SIZE ] = { 1, 3, 5, 4, 7, 2, 99, 16, 45, 67, 89, 45 };
11    int i;          /* counter */
12    int total = 0; /* sum of array */
13
14    /* sum contents of array a */
15    for ( i = 0; i < SIZE; i++ ) {
16        total += a[ i ];
17    } /* end for */
18
19    printf( "Total of array element values is %d\n", total );
20
21    return 0; /* indicates successful termination */
22
23 } /* end main */

```

Program Output

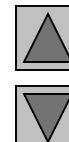
Total of array element values is 383

```
1 /* Fig. 6.7: fig06_07.c
2  Student poll program */
3 #include <stdio.h>
4 #define RESPONSE_SIZE 40 /* define array sizes */
5 #define FREQUENCY_SIZE 11
6
7 /* function main begins program execution */
8 int main()
9 {
10    int answer; /* counter */
11    int rating; /* counter */
12
13    /* initialize frequency counters to 0 */
14    int frequency[ FREQUENCY_SIZE ] = { 0 };
15
16    /* place survey responses in array responses */
17    int responses[ RESPONSE_SIZE ] = { 1, 2, 6, 4, 8, 5, 9, 7, 8, 10,
18        1, 6, 3, 8, 6, 10, 3, 8, 2, 7, 6, 5, 7, 6, 8, 6, 7, 5, 6, 6,
19        5, 6, 7, 5, 6, 4, 8, 6, 8, 10 };
```



Outline

fig06_07.c (Part 1 of 2)



Outline

fig06_07.c (Part 2 of 2)

```

21 /* for each answer, select value of an element of array responses
22     and use that value as subscript in array frequency to
23     determine element to increment */
24 for ( answer = 0; answer < RESPONSE_SIZE; answer++ ) {
25     ++frequency[ responses [ answer ] ];
26 } /* end for */

27

28 /* display results */
29 printf( "%s%17s\n", "Rating", "Frequency" );

30

31 /* output frequencies in tabular format */
32 for ( rating = 1; rating < FREQUENCY_SIZE; rating++ ) {
33     printf( "%6d%17d\n", rating, frequency[ rating ] );
34 } /* end for */

35

36 return 0; /* indicates successful termination */
37

38 } /* end main */

```

| Rating | Frequency |
|--------|-----------|
| 1 | 2 |
| 2 | 2 |
| 3 | 2 |
| 4 | 2 |
| 5 | 5 |
| 6 | 11 |
| 7 | 5 |
| 8 | 7 |
| 9 | 1 |
| 10 | 3 |

Program Output



Outline

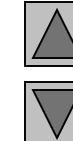
fig06_08.c (Part 1 of 2)

```

1 /* Fig. 6.8: fig06_08.c
2     Histogram printing program */
3 #include <stdio.h>
4 #define SIZE 10
5
6 /* function main begins program execution */
7 int main()
8 {
9     /* use initializer list to initialize array n */
10    int n[ SIZE ] = { 19, 3, 15, 7, 11, 9, 13, 5, 17, 1 };
11    int i; /* outer counter */
12    int j; /* inner counter */
13
14    printf( "%s%13s%17s\n", "Element", "Value", "Histogram" );
15
16    /* for each element of array n, output a bar in histogram */
17    for ( i = 0; i < SIZE; i++ ) {
18        printf( "%7d%13d      ", i, n[ i ] );
19
20        for ( j = 1; j <= n[ i ]; j++ ) { /* print one bar */
21            printf( "%c", '*' );
22        } /* end inner for */
23    }

```

```
24     printf( "\n" ); /* start next line of output */
25 } /* end outer for */
26
27 return 0; /* indicates successful termination */
28
29 } /* end main */
```



Outline

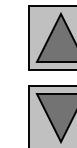


fig06_08.c (Part 2 of 2)

Program Output

| Element | value | Histogram |
|---------|-------|-----------|
| 0 | 19 | ***** |
| 1 | 3 | *** |
| 2 | 15 | ***** |
| 3 | 7 | ***** |
| 4 | 11 | ***** |
| 5 | 9 | ***** |
| 6 | 13 | ***** |
| 7 | 5 | *** |
| 8 | 17 | ***** |
| 9 | 1 | * |

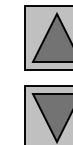
```
1 /* Fig. 6.9: fig06_09.c
2     Roll a six-sided die 6000 times */
3 #include <stdio.h>
4 #include <stdlib.h>
5 #include <time.h>
6 #define SIZE 7
7
8 /* function main begins program execution */
9 int main()
10 {
11     int face;                  /* random number with value 1 - 6 */
12     int roll;                 /* roll counter */
13     int frequency[ SIZE ] = { 0 }; /* initialize array to 0 */
14
15     srand( time( NULL ) ); /* seed random-number generator */
16
17     /* roll die 6000 times */
18     for ( roll = 1; roll <= 6000; roll++ ) {
19         face = rand() % 6 + 1;
20         ++frequency[ face ]; /* replaces 26-line switch of Fig. 5.8 */
21     } /* end for */
22
23     printf( "%s%17s\n", "Face", "Frequency" );
24 }
```



Outline

fig06_09.c (Part 1 of 2)

```
25 /* output frequency elements 1-6 in tabular format */  
26 for ( face = 1; face < SIZE; face++ ) {  
27     printf( "%4d%17d\n", face, frequency[ face ] );  
28 } /* end for */  
29  
30 return 0; /* indicates successful termination */  
31  
32 } /* end main */
```



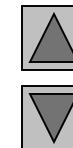
Outline

fig06_09.c (Part 2 of 2)

Program Output

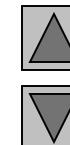
| Face | Frequency |
|------|-----------|
| 1 | 1029 |
| 2 | 951 |
| 3 | 987 |
| 4 | 1033 |
| 5 | 1010 |
| 6 | 990 |

```
1 /* Fig. 6.10: fig06_10.c
2  Treating character arrays as strings */
3 #include <stdio.h>
4
5 /* function main begins program execution */
6 int main()
7 {
8     char string1[ 20 ];           /* reserves 20 characters */
9     char string2[] = "string literal"; /* reserves 15 characters */
10    int i;                      /* counter */
11
12    /* read string from user into array string2 */
13    printf("Enter a string: ");
14    scanf( "%s", string1 );
15
16    /* output strings */
17    printf( "string1 is: %s\nstring2 is: %s\n"
18           "string1 with spaces between characters is:\n",
19           string1, string2 );
20
21    /* output characters until null character is reached */
22    for ( i = 0; string1[ i ] != '\0'; i++ ) {
23        printf( "%c ", string1[ i ] );
24    } /* end for */
25
```



Outline

fig06_10.c (Part 1 of 2)



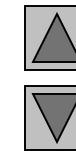
Outline

```
26 printf( "\n" );
27
28 return 0; /* indicates successful termination */
29
30 } /* end main */
```

```
Enter a string: Hello there
string1 is: Hello
string2 is: string literal
string1 with spaces between characters is:
H e l l o
```

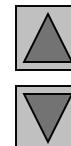
fig06_10.c (Part 2 of 2)

```
1 /* Fig. 6.11: fig06_11.c
2  Static arrays are initialized to zero */
3 #include <stdio.h>
4
5 void staticArrayInit( void ); /* function prototype */
6 void automaticArrayInit( void ); /* function prototype */
7
8 /* function main begins program execution */
9 int main()
10 {
11     printf( "First call to each function:\n" );
12     staticArrayInit();
13     automaticArrayInit();
14
15     printf( "\n\nSecond call to each function:\n" );
16     staticArrayInit();
17     automaticArrayInit();
18
19     return 0; /* indicates successful termination */
20
21 } /* end main */
22
```



Outline

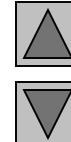
fig06_11.c (Part 1 of 3)



Outline

fig06_11.c (Part 2 of 3)

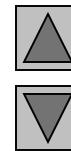
```
23 /* function to demonstrate a static local array */
24 void staticArrayInit( void )
25 {
26     /* initializes elements to 0 first time function is called */
27     static int array1[ 3 ];
28     int i; /* counter */
29
30     printf( "\nvalues on entering staticArrayInit:\n" );
31
32     /* output contents of array1 */
33     for ( i = 0; i <= 2; i++ ) {
34         printf( "array1[ %d ] = %d  ", i, array1[ i ] );
35     } /* end for */
36
37     printf( "\nvalues on exiting staticArrayInit:\n" );
38
39     /* modify and output contents of array1 */
40     for ( i = 0; i <= 2; i++ ) {
41         printf( "array1[ %d ] = %d  ", i, array1[ i ] += 5 );
42     } /* end for */
43
44 } /* end function staticArrayInit */
45
```



Outline

```
46 /* function to demonstrate an automatic local array */  
47 void automaticArrayInit( void )  
48 {  
49     /* initializes elements each time function is called */  
50     int array2[ 3 ] = { 1, 2, 3 };  
51     int i; /* counter */  
52  
53     printf( "\n\nvalues on entering automaticArrayInit:\n" );  
54  
55     /* output contents of array2 */  
56     for ( i = 0; i <= 2; i++ ) {  
57         printf("array2[ %d ] = %d ", i, array2[ i ] );  
58     } /* end for */  
59  
60     printf( "\nvalues on exiting automaticArrayInit:\n" );  
61  
62     /* modify and output contents of array2 */  
63     for ( i = 0; i <= 2; i++ ) {  
64         printf( "array2[ %d ] = %d ", i, array2[ i ] += 5 );  
65     } /* end for */  
66  
67 } /* end function automaticArrayInit */
```

fig06_11.c (Part 3 of 3)



Outline

Program Output

First call to each function:

values on entering staticArrayInit:

array1[0] = 0 array1[1] = 0 array1[2] = 0

values on exiting staticArrayInit:

array1[0] = 5 array1[1] = 5 array1[2] = 5

values on entering automaticArrayInit:

array2[0] = 1 array2[1] = 2 array2[2] = 3

values on exiting automaticArrayInit:

array2[0] = 6 array2[1] = 7 array2[2] = 8

Second call to each function:

values on entering staticArrayInit:

array1[0] = 5 array1[1] = 5 array1[2] = 5

values on exiting staticArrayInit:

array1[0] = 10 array1[1] = 10 array1[2] = 10

values on entering automaticArrayInit:

array2[0] = 1 array2[1] = 2 array2[2] = 3

values on exiting automaticArrayInit:

array2[0] = 6 array2[1] = 7 array2[2] = 8

6.5 Passing Arrays to Functions

- Passing arrays
 - To pass an array argument to a function, specify the name of the array without any brackets

```
int myArray[ 24 ];  
myFunction( myArray, 24 );
```

 - Array size usually passed to function
 - Arrays passed call-by-reference
 - Name of array is address of first element
 - Function knows where the array is stored
 - Modifies original memory locations
- Passing array elements
 - Passed by call-by-value
 - Pass subscripted name (i.e., `myArray[3]`) to function



6.5 Passing Arrays to Functions

- Function prototype

```
void modifyArray( int b[], int arraySize );
```

- Parameter names optional in prototype
 - `int b[]` could be written `int []`
 - `int arraySize` could be simply `int`



Outline

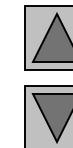
```
1 /* Fig. 6.12: fig06_12.c
2   The name of an array is the same as &array[ 0 ] */
3 #include <stdio.h>
4
5 /* function main begins program execution */
6 int main()
7 {
8     char array[ 5 ]; /* define an array of size 5 */
9
10    printf( "    array = %p\n&array[0] = %p\n"
11           "    &array = %p\n",
12           array, &array[ 0 ], &array );
13
14    return 0; /* indicates successful termination */
15
16 } /* end main */
```

array = 0012FF78
&array[0] = 0012FF78
 &array = 0012FF78

fig06_12.c

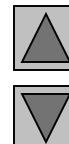
Program Output

```
1 /* Fig. 6.13: fig06_13.c
2  Passing arrays and individual array elements to functions */
3 #include <stdio.h>
4 #define SIZE 5
5
6 /* function prototypes */
7 void modifyArray( int b[], int size );
8 void modifyElement( int e );
9
10 /* function main begins program execution */
11 int main()
12 {
13     int a[ SIZE ] = { 0, 1, 2, 3, 4 }; /* initialize a */
14     int i; /* counter */
15
16     printf( "Effects of passing entire array by reference:\n\nThe "
17             "values of the original array are:\n" );
18
19     /* output original array */
20     for ( i = 0; i < SIZE; i++ ) {
21         printf( "%3d", a[ i ] );
22     } /* end for */
23
24     printf( "\n" );
25 }
```



Outline

fig06_13.c (Part 1 of 3)



Outline

fig06_13.c (Part 2 of 3)

```
26 /* pass array a to modifyArray by reference */
27 modifyArray( a, SIZE );
28
29 printf( "The values of the modified array are:\n" );
30
31 /* output modified array */
32 for ( i = 0; i < SIZE; i++ ) {
33     printf( "%3d", a[ i ] );
34 } /* end for */
35
36 /* output value of a[ 3 ] */
37 printf( "\n\nEffects of passing array element "
38         "by value:\n\nThe value of a[3] is %d\n", a[ 3 ] );
39
40 modifyElement( a[ 3 ] ); /* pass array element a[ 3 ] by value */
41
42 /* output value of a[ 3 ] */
43 printf( "The value of a[ 3 ] is %d\n", a[ 3 ] );
44
45 return 0; /* indicates successful termination */
46
47 } /* end main */
48
```



Outline

fig06_13.c (Part 3 of 3)

```
49 /* in function modifyArray, "b" points to the original array "a"
50   in memory */
51 void modifyArray( int b[], int size )
52 {
53     int j; /* counter */
54
55     /* multiply each array element by 2 */
56     for ( j = 0; j < size; j++ ) {
57         b[ j ] *= 2;
58     } /* end for */
59
60 } /* end function modifyArray */
61
62 /* in function modifyElement, "e" is a local copy of array element
63   a[ 3 ] passed from main */
64 void modifyElement( int e )
65 {
66     /* multiply parameter by 2 */
67     printf( "Value in modifyElement is %d\n", e *= 2 );
68 } /* end function modifyElement */
```

Effects of passing entire array by reference:

The values of the original array are:

0 1 2 3 4

The values of the modified array are:

0 2 4 6 8



Outline

Program Output

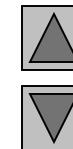
Effects of passing array element by value:

The value of a[3] is 6

value in modifyElement is 12

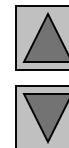
The value of a[3] is 6

```
1 /* Fig. 6.14: fig06_14.c
2 Demonstrating the const type qualifier with arrays */
3 #include <stdio.h>
4
5 void tryToModifyArray( const int b[] ); /* function prototype */
6
7 /* function main begins program execution */
8 int main()
9 {
10     int a[] = { 10, 20, 30 }; /* initialize a */
11
12     tryToModifyArray( a );
13
14     printf("%d %d %d\n", a[ 0 ], a[ 1 ], a[ 2 ] );
15
16     return 0; /* indicates successful termination */
17
18 } /* end main */
19
```



Outline

fig06_14.c (Part 1 of 2)



Outline

fig06_14.c (Part 2 of 2)

```
20 /* in function tryToModifyArray, array b is const, so it cannot be
21     used to modify the original array a in main. */
22 void tryToModifyArray( const int b[] )
23 {
24     b[ 0 ] /= 2;      /* error */
25     b[ 1 ] /= 2;      /* error */
26     b[ 2 ] /= 2;      /* error */
27 } /* end function tryToModifyArray */
```

Compiling...

FIG06_14.C

```
fig06_14.c(24) : error C2166: l-value specifies const object
fig06_14.c(25) : error C2166: l-value specifies const object
fig06_14.c(26) : error C2166: l-value specifies const object
```

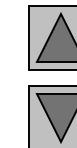
Program Output

6.6 Sorting Arrays

- Sorting data
 - Important computing application
 - Virtually every organization must sort some data
 - Bubble sort (sinking sort)
 - Several passes through the array
 - Successive pairs of elements are compared
 - If increasing order (or identical), no change
 - If decreasing order, elements exchanged
 - Repeat
 - Example:
 - original: 3 4 2 6 7
 - pass 1: 3 **2 4** 6 7
 - pass 2: **2 3** 4 6 7
 - Small elements "bubble" to the top
- © Copyright 1992–2004 by Deitel & Associates, Inc. and Pearson Education, Inc. All Rights Reserved.

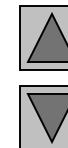


```
1 /* Fig. 6.15: fig06_15.c
2  This program sorts an array's values into ascending order */
3 #include <stdio.h>
4 #define SIZE 10
5
6 /* function main begins program execution */
7 int main()
8 {
9     /* initialize a */
10    int a[ SIZE ] = { 2, 6, 4, 8, 10, 12, 89, 68, 45, 37 };
11    int i;      /* inner counter */
12    int pass; /* outer counter */
13    int hold; /* temporary location used to swap array elements */
14
15    printf( "Data items in original order\n" );
16
17    /* output original array */
18    for ( i = 0; i < SIZE; i++ ) {
19        printf( "%4d", a[ i ] );
20    } /* end for */
21}
```



Outline

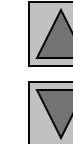
fig06_15.c (Part 1 of 3)



Outline

fig06_15.c (Part 2 of 3)

```
22 /* bubble sort */
23 /* loop to control number of passes */
24 for ( pass = 1; pass < SIZE; pass++ ) {
25
26     /* loop to control number of comparisons per pass */
27     for ( i = 0; i < SIZE - 1; i++ ) {
28
29         /* compare adjacent elements and swap them if first
30         element is greater than second element */
31         if ( a[ i ] > a[ i + 1 ] ) {
32             hold = a[ i ];
33             a[ i ] = a[ i + 1 ];
34             a[ i + 1 ] = hold;
35         } /* end if */
36
37     } /* end inner for */
38
39 } /* end outer for */
40
41 printf( "\nData items in ascending order\n" );
42
```



Outline

fig06_15.c (Part 3 of 3)

```
43 /* output sorted array */
44 for ( i = 0; i < SIZE; i++ ) {
45     printf( "%4d", a[ i ] );
46 } /* end for */
47
48 printf( "\n" );
49
50 return 0; /* indicates successful termination */
51
```

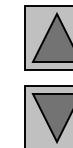
```
Data items in original order
 2   6   4   8  10  12  89  68  45  37
Data items in ascending order
 2   4   6   8  10  12  37  45  68  89
```

Program Output

6.7 Case Study: Computing Mean, Median and Mode Using Arrays

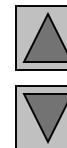
- Mean – average
- Median – number in middle of sorted list
 - 1, 2, 3, 4, 5
 - 3 is the median
- Mode – number that occurs most often
 - 1, 1, 1, 2, 3, 3, 4, 5
 - 1 is the mode

```
1 /* Fig. 6.16: fig06_16.c
2  This program introduces the topic of survey data analysis.
3  It computes the mean, median, and mode of the data */
4 #include <stdio.h>
5 #define SIZE 99
6
7 /* function prototypes */
8 void mean( const int answer[] );
9 void median( int answer[] );
10 void mode( int freq[], const int answer[] );
11 void bubbleSort( int a[] );
12 void printArray( const int a[] );
13
14 /* function main begins program execution */
15 int main()
16 {
17     int frequency[ 10 ] = { 0 }; /* initialize array frequency */
18 }
```



Outline

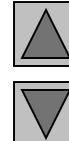
fig06_16.c (Part 1 of 8)



Outline

fig06_16.c (Part 2 of 8)

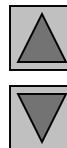
```
19 /* initialize array response */
20 int response[ SIZE ] =
21 { 6, 7, 8, 9, 8, 7, 8, 9, 8, 9,
22   7, 8, 9, 5, 9, 8, 7, 8, 7, 8,
23   6, 7, 8, 9, 3, 9, 8, 7, 8, 7,
24   7, 8, 9, 8, 9, 8, 9, 7, 8, 9,
25   6, 7, 8, 7, 8, 7, 9, 8, 9, 2,
26   7, 8, 9, 8, 9, 8, 9, 7, 5, 3,
27   5, 6, 7, 2, 5, 3, 9, 4, 6, 4,
28   7, 8, 9, 6, 8, 7, 8, 9, 7, 8,
29   7, 4, 4, 2, 5, 3, 8, 7, 5, 6,
30   4, 5, 6, 1, 6, 5, 7, 8, 7 };
31
32 /* process responses */
33 mean( response );
34 median( response );
35 mode( frequency, response );
36
37 return 0; /* indicates successful termination */
38
39 } /* end main */
40
```



Outline

fig06_16.c (Part 3 of 8)

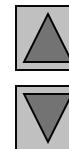
```
41 /* calculate average of all response values */
42 void mean( const int answer[] )
43 {
44     int j;           /* counter */
45     int total = 0; /* variable to hold sum of array elements */
46
47     printf( "%s\n%s\n%s\n", "*****", " Mean", "*****" );
48
49     /* total response values */
50     for ( j = 0; j < SIZE; j++ ) {
51         total += answer[ j ];
52     } /* end for */
53
54     printf( "The mean is the average value of the data\n"
55             "items. The mean is equal to the total of\n"
56             "all the data items divided by the number\n"
57             "of data items ( %d ). The mean value for\n"
58             "this run is: %d / %d = %.4f\n\n",
59             SIZE, total, SIZE, ( double ) total / SIZE );
60 } /* end function mean */
61
```



Outline

fig06_16.c (Part 4 of 8)

```
62 /* sort array and determine median element's value */
63 void median( int answer[] )
64 {
65     printf( "\n%s\n%s\n%s\n%s",
66             "*****", " Median", "*****",
67             "The unsorted array of responses is" );
68
69     printArray( answer ); /* output unsorted array */
70
71     bubbleSort( answer ); /* sort array */
72
73     printf( "\n\nThe sorted array is" );
74     printArray( answer ); /* output sorted array */
75
76     /* display median element */
77     printf( "\n\nThe median is element %d of\n"
78             "the sorted %d element array.\n"
79             "For this run the median is %d\n\n",
80             SIZE / 2, SIZE, answer[ SIZE / 2 ] );
81 } /* end function median */
82
```



Outline

fig06_16.c (Part 5 of 8)

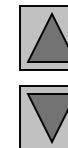
```
83 /* determine most frequent response */
84 void mode( int freq[], const int answer[] )
85 {
86     int rating;          /* counter */
87     int j;               /* counter */
88     int h;               /* counter */
89     int largest = 0;     /* represents largest frequency */
90     int modeValue = 0;   /* represents most frequent response */
91
92     printf( "\n%s\n%s\n%s\n",
93             "*****", " Mode", "*****" );
94
95     /* initialize frequencies to 0 */
96     for ( rating = 1; rating <= 9; rating++ ) {
97         freq[ rating ] = 0;
98     } /* end for */
99
100    /* summarize frequencies */
101    for ( j = 0; j < SIZE; j++ ) {
102        ++freq[ answer[ j ] ];
103    } /* end for */
104
```



Outline

fig06_16.c (Part 6 of 8)

```
105 /* output headers for result columns */
106 printf( "%s%11s%19s\n\n%54s\n%54s\n\n",
107         "Response", "Frequency", "Histogram",
108         "1      1      2      2", "5      0      5      0      5" );
109
110 /* output results */
111 for ( rating = 1; rating <= 9; rating++ ) {
112     printf( "%8d%11d          ", rating, freq[ rating ] );
113
114     /* keep track of mode value and largest frequency value */
115     if ( freq[ rating ] > largest ) {
116         largest = freq[ rating ];
117         modeValue = rating;
118     } /* end if */
119
120     /* output histogram bar representing frequency value */
121     for ( h = 1; h <= freq[ rating ]; h++ ) {
122         printf( "*" );
123     } /* end inner for */
124
125     printf( "\n" ); /* begin new line of output */
126 } /* end outer for */
127
```



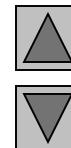
Outline

fig06_16.c (Part 7 of 8)

```

128 /* display the mode value */
129 printf( "The mode is the most frequent value.\n"
130         "For this run the mode is %d which occurred"
131         " %d times.\n", modevalue, largest );
132} /* end function mode */
133
134/* function that sorts an array with bubble sort algorithm */
135void bubbleSort( int a[] )
136{
137    int pass; /* counter */
138    int j;    /* counter */
139    int hold; /* temporary location used to swap elements */
140
141    /* loop to control number of passes */
142    for ( pass = 1; pass < SIZE; pass++ ) {
143
144        /* loop to control number of comparisons per pass */
145        for ( j = 0; j < SIZE - 1; j++ ) {
146
147            /* swap elements if out of order */
148            if ( a[ j ] > a[ j + 1 ] ) {
149                hold = a[ j ];
150                a[ j ] = a[ j + 1 ];
151                a[ j + 1 ] = hold;
152            } /* end if */
153

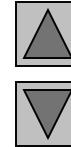
```



Outline

```
154 } /* end inner for */  
155  
156 } /* end outer for */  
157  
158} /* end function bubbleSort */  
159  
160/* output array contents (20 values per row) */  
161void printArray( const int a[] )  
162{  
163     int j; /* counter */  
164  
165     /* output array contents */  
166     for ( j = 0; j < SIZE; j++ ) {  
167  
168         if ( j % 20 == 0 ) { /* begin new line every 20 values */  
169             printf( "\n" );  
170         } /* end if */  
171  
172         printf( "%2d", a[ j ] );  
173     } /* end for */  
174  
175} /* end function printArray */
```

fig06_16.c (Part 8 of 8)



Outline

Program Output

Mean

The mean is the average value of the data items. The mean is equal to the total of all the data items divided by the number of data items (99). The mean value for this run is: $681 / 99 = 6.8788$

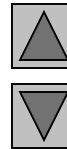
Median

The unsorted array of responses is

6 7 8 9 8 7 8 9 8 9 7 8 9 5 9 8 7 8 7 8
6 7 8 9 3 9 8 7 8 7 7 8 9 8 9 8 9 7 8 9
6 7 8 7 8 7 9 8 9 2 7 8 9 8 9 8 9 7 5 3
5 6 7 2 5 3 9 4 6 4 7 8 9 6 8 7 8 9 7 8
7 4 4 2 5 3 8 7 5 6 4 5 6 1 6 5 7 8 7

The sorted array is

1 2 2 2 3 3 3 3 4 4 4 4 4 5 5 5 5 5 5 5
5 6 6 6 6 6 6 6 6 7 7 7 7 7 7 7 7 7 7 7
7 7 7 7 7 7 7 7 7 7 7 7 8 8 8 8 8 8 8 8
8
9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9



Outline

The median is element 49 of
the sorted 99 element array.
For this run the median is 7

Program Output (continued)

Mode

| Response | Frequency | Histogram |
|----------|-----------|-----------|
|----------|-----------|-----------|

| | | | | |
|---|---|---|---|---|
| 5 | 1 | 1 | 2 | 2 |
| 0 | 5 | 0 | 5 | |

| | | |
|---|----|-------|
| 1 | 1 | * |
| 2 | 3 | *** |
| 3 | 4 | **** |
| 4 | 5 | ***** |
| 5 | 8 | ***** |
| 6 | 9 | ***** |
| 7 | 23 | ***** |
| 8 | 27 | ***** |
| 9 | 19 | ***** |

The mode is the most frequent value.

For this run the mode is 8 which occurred 27 times.

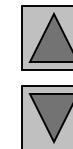
6.8 Searching Arrays: Linear Search and Binary Search

- Search an array for a *key value*
- Linear search
 - Simple
 - Compare each element of array with key value
 - Useful for small and unsorted arrays

6.8 Searching Arrays: Linear Search and Binary Search

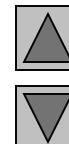
- Binary search
 - For sorted arrays
 - Compares `middle` element with `key`
 - If equal, match found
 - If `key < middle`, looks in first half of array
 - If `key > middle`, looks in last half
 - Repeat
 - Very fast; at most n steps, where $2^n >$ number of elements
 - 30 element array takes at most 5 steps
 - $2^5 > 30$ so at most 5 steps

```
1 /* Fig. 6.18: fig06_18.c
2  Linear search of an array */
3 #include <stdio.h>
4 #define SIZE 100
5
6 /* function prototype */
7 int linearSearch( const int array[], int key, int size );
8
9 /* function main begins program execution */
10 int main()
11 {
12     int a[ SIZE ]; /* create array a */
13     int x;          /* counter */
14     int searchKey; /* value to locate in a */
15     int element;   /* variable to hold location of searchKey or -1 */
16
17     /* create data */
18     for ( x = 0; x < SIZE; x++ ) {
19         a[ x ] = 2 * x;
20     } /* end for */
21
22     printf( "Enter integer search key:\n" );
23     scanf( "%d", &searchKey );
24 }
```



Outline

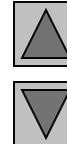
fig06_18.c (Part 1 of 3)



Outline

fig06_18.c (Part 2 of 3)

```
25 /* attempt to locate searchKey in array a */
26 element = linearSearch( a, searchKey, SIZE );
27
28 /* display results */
29 if ( element != -1 ) {
30     printf( "Found value in element %d\n", element );
31 } /* end if */
32 else {
33     printf( "value not found\n" );
34 } /* end else */
35
36 return 0; /* indicates successful termination */
37
38 } /* end main */
39
40 /* compare key to every element of array until the location is found
41 or until the end of array is reached; return subscript of element
42 if key or -1 if key is not found */
43 int linearSearch( const int array[], int key, int size )
44 {
45     int n; /* counter */
46
47     /* Loop through array */
48     for ( n = 0; n < size; ++n ) {
49 }
```



Outline

fig06_18.c (Part 3 of 3)

Program Output

```
Enter integer search key:
```

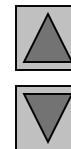
```
36
```

```
Found value in element 18
```

```
Enter integer search key:
```

```
37
```

```
Value not found
```



Outline

fig06_19.c (Part 1 of 5)

```

1 /* Fig. 6.19: fig06_19.c
2     Binary search of an array */
3 #include <stdio.h>
4 #define SIZE 15
5
6 /* function prototypes */
7 int binarySearch( const int b[], int searchKey, int low, int high );
8 void printHeader( void );
9 void printRow( const int b[], int low, int mid, int high );
10
11 /* function main begins program execution */
12 int main()
13 {
14     int a[ SIZE ]; /* create array a */
15     int i;          /* counter */
16     int key;        /* value to locate in array a */
17     int result;     /* variable to hold location of key or -1 */
18
19     /* create data */
20     for ( i = 0; i < SIZE; i++ ) {
21         a[ i ] = 2 * i;
22     } /* end for */
23
24     printf( "Enter a number between 0 and 28: " );
25     scanf( "%d", &key );
26

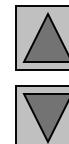
```



Outline

fig06_19.c (Part 2 of 5)

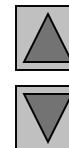
```
27 printHeader();  
28  
29 /* search for key in array a */  
30 result = binarySearch( a, key, 0, SIZE - 1 );  
31  
32 /* display results */  
33 if ( result != -1 ) {  
34     printf( "\n%d found in array element %d\n", key, result );  
35 } /* end if */  
36 else {  
37     printf( "\n%d not found\n", key );  
38 } /* end else */  
39  
40 return 0; /* indicates successful termination */  
41  
42 } /* end main */  
43  
44 /* function to perform binary search of an array */  
45 int binarySearch( const int b[], int searchKey, int low, int high )  
46 {  
47     int middle; /* variable to hold middle element of array */  
48
```



Outline

fig06_19.c (Part 3
of 5)

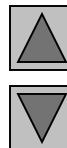
```
49 /* Loop until low subscript is greater than high subscript */
50 while ( low <= high ) {
51
52     /* determine middle element of subarray being searched */
53     middle = ( low + high ) / 2;
54
55     /* display subarray used in this loop iteration */
56     printRow( b, low, middle, high );
57
58     /* if searchKey matched middle element, return middle */
59     if ( searchKey == b[ middle ] ) {
60         return middle;
61     } /* end if */
62
63     /* if searchKey less than middle element, set new high */
64     else if ( searchKey < b[ middle ] ) {
65         high = middle - 1; /* search low end of array */
66     } /* end else if */
67
68     /* if searchKey greater than middle element, set new low */
69     else {
70         low = middle + 1; /* search high end of array */
71     } /* end else */
72
73 } /* end while */
74
```



Outline

fig06_19.c (Part 4 of 5)

```
75     return -1; /* searchKey not found */
76
77 } /* end function binarySearch */
78
79 /* Print a header for the output */
80 void printHeader( void )
81 {
82     int i; /* counter */
83
84     printf( "\nSubscripts:\n" );
85
86     /* output column head */
87     for ( i = 0; i < SIZE; i++ ) {
88         printf( "%3d ", i );
89     } /* end for */
90
91     printf( "\n" ); /* start new line of output */
92
93     /* output line of - characters */
94     for ( i = 1; i <= 4 * SIZE; i++ ) {
95         printf( "-" );
96     } /* end for */
97
98     printf( "\n" ); /* start new line of output */
99 } /* end function printHeader */
100
```



Outline

fig06_19.c (Part 5 of 5)

```
101/* Print one row of output showing the current
102 part of the array being processed. */
103void printRow( const int b[], int low, int mid, int high )
104{
105    int i; /* counter */
106
107    /* Loop through entire array */
108    for ( i = 0; i < SIZE; i++ ) {
109
110        /* display spaces if outside current subarray range */
111        if ( i < low || i > high ) {
112            printf( "    " );
113        } /* end if */
114        else if ( i == mid ) { /* display middle element */
115            printf( "%3d*", b[ i ] ); /* mark middle value */
116        } /* end else if */
117        else { /* display other elements in subarray */
118            printf( "%3d ", b[ i ] );
119        } /* end else */
120
121    } /* end for */
122
123    printf( "\n" ); /* start new line of output */
124} /* end function printRow */
```



Outline

Program Output

Enter a number between 0 and 28: 25

Subscripts:

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14

0 2 4 6 8 10 12 14* 16 18 20 22 24 26 28
16 18 20 22* 24 26 28
24 26* 28
24*

25 not found

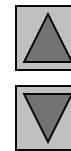
Enter a number between 0 and 28: 8

Subscripts:

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14

0 2 4 6 8 10 12 14* 16 18 20 22 24 26 28
0 2 4 6* 8 10 12
8 10* 12
8*

8 found in array element 4



Outline

Enter a number between 0 and 28: 6

Subscripts:

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14

0 2 4 6 8 10 12 14* 16 18 20 22 24 26 28

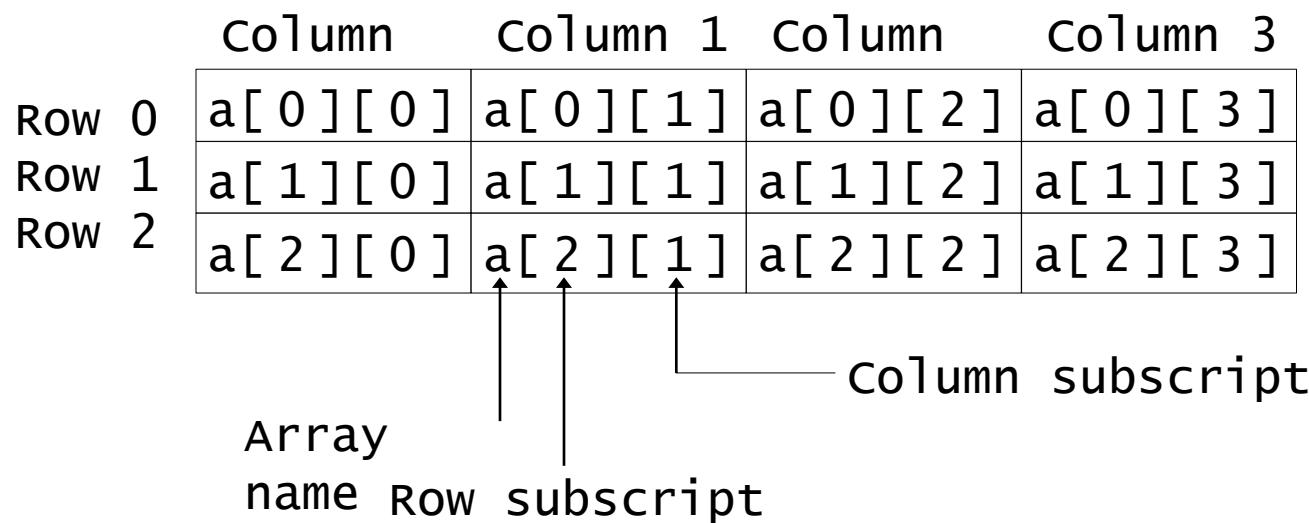
0 2 4 6* 8 10 12

**Program Output
(continued)**

6 found in array element 3

6.9 Multiple-Subscripted Arrays

- Multiple subscripted arrays
 - Tables with rows and columns (m by n array)
 - Like matrices: specify row, then column



6.9 Multiple-Subscripted Arrays

- Initialization

- `int b[2][2] = { { 1, 2 }, { 3, 4 } };`
 - Initializers grouped by row in braces
 - If not enough, unspecified elements set to zero

```
int b[ 2 ][ 2 ] = { { 1 }, { 3, 4 } };
```

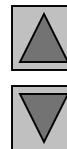
| | |
|---|---|
| 1 | 2 |
| 3 | 4 |

- Referencing elements

- Specify row, then column

```
printf( "%d", b[ 0 ][ 1 ] );
```

| | |
|---|---|
| 1 | 0 |
| 3 | 4 |



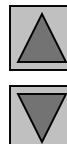
Outline

fig06_21.c (Part 1 of 2)

```

1 /* Fig. 6.21: fig06_21.c
2     Initializing multidimensional arrays */
3 #include <stdio.h>
4
5 void printArray( const int a[][ 3 ] ); /* function prototype */
6
7 /* function main begins program execution */
8 int main()
9 {
10     /* initialize array1, array2, array3 */
11     int array1[ 2 ][ 3 ] = { { 1, 2, 3 }, { 4, 5, 6 } };
12     int array2[ 2 ][ 3 ] = { { 1, 2, 3, 4, 5 } };
13     int array3[ 2 ][ 3 ] = { { { 1, 2 }, { 4 } } };
14
15     printf( "values in array1 by row are:\n" );
16     printArray( array1 );
17
18     printf( "values in array2 by row are:\n" );
19     printArray( array2 );
20
21     printf( "values in array3 by row are:\n" );
22     printArray( array3 );
23
24     return 0; /* indicates successful termination */
25
26 } /* end main */
27

```



Outline

fig06_21.c (Part 2 of 2)

```

28 /* function to output array with two rows and three columns */
29 void printArray( const int a[][][ 3 ] )
30 {
31     int i; /* counter */
32     int j; /* counter */
33
34     /* Loop through rows */
35     for ( i = 0; i <= 1; i++ ) {
36
37         /* output column values */
38         for ( j = 0; j <= 2; j++ ) {
39             printf( "%d ", a[ i ][ j ] );
40         } /* end inner for */
41
42         printf( "\n" ); /* start new line of output */
43     } /* end outer for */
44
45 } /* end function printArray */

```

values in array1 by row are:

1 2 3

4 5 6

values in array2 by row are:

1 2 3

4 5 0

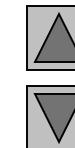
values in array3 by row are:

1 2 0

4 0 0

Program Output

```
1 /* Fig. 6.22: fig06_22.c
2  Double-subscripted array example */
3 #include <stdio.h>
4 #define STUDENTS 3
5 #define EXAMS 4
6
7 /* function prototypes */
8 int minimum( const int grades[][ EXAMS ], int pupils, int tests );
9 int maximum( const int grades[][ EXAMS ], int pupils, int tests );
10 double average( const int setOfGrades[], int tests );
11 void printArray( const int grades[][ EXAMS ], int pupils, int tests );
12
13 /* function main begins program execution */
14 int main()
15 {
16     int student; /* counter */
17
18     /* initialize student grades for three students (rows) */
19     const int studentGrades[ STUDENTS ][ EXAMS ] =
20         { { 77, 68, 86, 73 },
21           { 96, 87, 89, 78 },
22           { 70, 90, 86, 81 } };
23 }
```



Outline

fig06_22.c (Part 1 of 6)



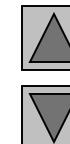
Outline

```

24 /* output array studentGrades */
25 printf( "The array is:\n" );
26 printArray( studentGrades, STUDENTS, EXAMS );
27
28 /* determine smallest and largest grade values */
29 printf( "\n\nLowest grade: %d\nHighest grade: %d\n",
30     minimum( studentGrades, STUDENTS, EXAMS ),
31     maximum( studentGrades, STUDENTS, EXAMS ) );
32
33 /* calculate average grade for each student */
34 for ( student = 0; student <= STUDENTS - 1; student++ ) {
35     printf( "The average grade for student %d is %.2f\n",
36         student, average( studentGrades[ student ], EXAMS ) );
37 } /* end for */
38
39 return 0; /* indicates successful termination */
40
41 } /* end main */
42
43 /* Find the minimum grade */
44 int minimum( const int grades[][ EXAMS ], int pupils, int tests )
45 {
46     int i;          /* counter */
47     int j;          /* counter */
48     int lowGrade = 100; /* initialize to highest possible grade */
49

```

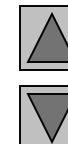
fig06_22.c (Part 2 of 6)



Outline

fig06_22.c (Part 3 of 6)

```
50 /* Loop through rows of grades */
51 for ( i = 0; i < pupils; i++ ) {
52
53     /* Loop through columns of grades */
54     for ( j = 0; j < tests; j++ ) {
55
56         if ( grades[ i ][ j ] < lowGrade ) {
57             lowGrade = grades[ i ][ j ];
58         } /* end if */
59
60     } /* end inner for */
61
62 } /* end outer for */
63
64 return lowGrade; /* return minimum grade */
65
66 } /* end function minimum */
67
68 /* Find the maximum grade */
69 int maximum( const int grades[][][ EXAMS ], int pupils, int tests )
70 {
71     int i;                  /* counter */
72     int j;                  /* counter */
73     int highGrade = 0; /* initialize to lowest possible grade */
74 }
```



Outline

fig06_22.c (Part 4 of 6)

```
/* Loop through rows of grades */
for ( i = 0; i < pupils; i++ ) {

    /* Loop through columns of grades */
    for ( j = 0; j < tests; j++ ) {

        if ( grades[ i ][ j ] > highGrade ) {
            highGrade = grades[ i ][ j ];
        } /* end if */

    } /* end inner for */

} /* end outer for */

return highGrade; /* return maximum grade */

} /* end function maximum */

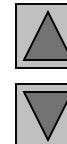
/* Determine the average grade for a particular student */
double average( const int setOfGrades[], int tests )
{
    int i;          /* counter */
    int total = 0; /* sum of test grades */
}
```



Outline

fig06_22.c (Part 5 of 6)

```
99  /* total all grades for one student */
100 for ( i = 0; i < tests; i++ ) {
101     total += setofGrades[ i ];
102 } /* end for */
103
104 return ( double ) total / tests; /* average */
105
106} /* end function average */
107
108/* Print the array */
109void printArray( const int grades[][][ EXAMS ], int pupils, int tests )
110{
111    int i; /* counter */
112    int j; /* counter */
113
114    /* output column heads */
115    printf( " [0] [1] [2] [3]" );
116
117    /* output grades in tabular format */
118    for ( i = 0; i < pupils; i++ ) {
119
120        /* output label for row */
121        printf( "\nstudentGrades[%d] ", i );
```



Outline

fig06_22.c (Part 6 of 6)

```
123     /* output grades for one student */
124     for ( j = 0; j < tests; j++ ) {
125         printf( "%-5d", grades[ i ][ j ] );
126     } /* end inner for */
127
128 } /* end outer for */
129
130} /* end function printArray */
```

The array is:

| | [0] | [1] | [2] | [3] |
|------------------|-----|-----|-----|-----|
| studentGrades[0] | 77 | 68 | 86 | 73 |
| studentGrades[1] | 96 | 87 | 89 | 78 |
| studentGrades[2] | 70 | 90 | 86 | 81 |

Lowest grade: 68

Highest grade: 96

The average grade for student 0 is 76.00

The average grade for student 1 is 87.50

The average grade for student 2 is 81.75